## **International Journal of Theoretical & Computational Physics**

# Exploring Fractal Quantum Field Theory in Higher-Order Dimensions Using the McGinty Equation

## **Chris McGinty**

Founder of Skywise.ai, Greater Minneapolis-St. Paul Area, USA.

\*Correspondence author Chris McGinty Founder of Skywise.ai, Greater Minneapolis-St. Paul Area, USA.

Submitted : 5 July 2024 ; Published : 27 Sept 2024

**Citation:** Chris McGinty(2024). Exploring Fractal Quantum Field Theory in Higher-Order Dimensions Using the McGinty Equation. I J T C Physics, Special Issue :1-2. DOI : https://doi.org/10.47485/2767-3901.1051

#### Abstract

This hypothesis investigates the application of the McGinty Equation to quantum fields in higher-order dimensions, proposing that these fields exhibit self-similar fractal properties. The primary objective is to understand the implications of fractal geometry on quantum field interactions, coupling constants, and particle scattering processes, offering new insights into the fundamental forces and the structure of spacetime.

#### Introduction

Quantum field theory (QFT) has long been a cornerstone in understanding the interactions of fundamental particles. However, traditional QFT in integer dimensions may not fully capture the complexities of space-time, especially at higher energies. This hypothesis extends QFT into fractal dimensions using the McGinty Equation, exploring the effects of fractal geometry on quantum fields.

## Mathematical Framework

## **Fractal-modified Quantum Field Action**

$$\begin{split} S[\phi] = \int d^{\Lambda}D \; x(\; 1/2 \; \partial_{\mu} \; \phi \; \partial^{\Lambda}\mu \; \phi \; - \; V(\phi)) \; . \; |x|^{\Lambda}(D\text{-}d) \\ \text{where } D \; \text{is the topological dimension, } d \; \text{is the fractal dimension,} \\ \text{and } |x|^{\Lambda}(D\text{-}d) \; \text{is the fractal measure.} \end{split}$$

## **Modified Propagator in Momentum Space**

$$\begin{split} G(p) &\sim 1 \; / \; (p^{2} + m^{2})^{\wedge}(D/(2d)) \\ \text{Fractal-corrected Coupling Constant Scaling} \\ g(\mu) &\sim \mu^{\wedge}(d\text{-}D) \; g\_0 \\ \text{where } \mu \text{ is the energy scale and } g\_0 \text{ is the bare coupling constant.} \end{split}$$

## Modified Renormalization Group Equation

 $\mu \ dg/d\mu = \beta(g) = -(d-D)g + b_0 \ g^3 + \dots$ 

#### Expected Results Particle Scattering Cross-Sections $\sigma(E) \sim E^{(2(d-D)/d)}$

**Field Correlation Functions**  $(\phi(x)\phi(0)) \sim |x|^{(-2(D-d))}$ 

#### **Running of Coupling Constants**

 $\alpha(Q^{2}) = \alpha(\mu^{2}) / (1 + \beta_{0} \alpha(\mu^{2}) \ln(Q^{2}/\mu^{2}))^{((D-d)/D)}$ 

where  $\alpha$  is the fine structure constant and Q is the momentum transfer.

## **Modification to the Casimir Effect**

 $F\_C \sim 1 \ / \ a^{(d+1)}$  where a is the plate separation, differing from the standard 1/  $a^{4}$  scaling.

## Fractal Dimension Estimation

 $d = \lim_{\epsilon \to 0} [\log N(\epsilon) / \log(1/\epsilon)]$ where N(\epsilon) is the number of boxes of size \epsilon needed to cover the field configuration.

## **Experimental Proposals**

- 1. High-Energy Particle Collisions: Investigate deviations from standard cross-section predictions at energies greater than 10 TeV.
- Precision Casimir Force Measurements: Measure the force between plates at separations from 10 nm to 1 μm, looking for fractal scaling.
- 3. Cosmic Ray Observations: Analyze the energy spectrum of ultra-high-energy cosmic rays for fractal scaling signatures.
- 4. Quantum Field Tomography: Develop techniques to reconstruct field configurations and analyze their fractal properties.

## **Computational Tasks**

- 1. Lattice Field Theory Simulations: Implement fractalmodified actions in lattice field theory simulations.
- 2. Monte Carlo Integration: Perform Monte Carlo integration of path integrals with fractal measures.
- 3. Numerical Solutions: Solve the modified renormalization group equations numerically.

#### **Theoretical Developments Needed**

- Formulate Ward-Takahashi identities in fractal space-time.
- Extend the Operator Product Expansion to incorporate fractal scaling.
- Develop fractal-modified BRST quantization for gauge theories.

#### **Key Research Focus Areas**

- Precision measurements of coupling constant running over a wide energy range.
- Development of new renormalization techniques for fractal field theories.
- Search for fractal patterns in high-energy scattering data and cosmic ray observations.
- Theoretical work on reconciling fractal QFT with fundamental symmetries and conservation laws.

#### Conclusion

This hypothesis proposes a groundbreaking framework for incorporating fractal dimensions into quantum field theory, potentially uncovering new facets of fundamental forces and spacetime structure. Experimental validation and theoretical advancements in this direction could significantly enhance our understanding of the universe's fundamental nature.

#### References

- McGinty, C. (2023). The McGinty Equation: Unifying Quantum Field Theory and Fractal Theory to Understand Subatomic Behavior. *International Journal of Theoretical* & Computational Physics, 5(2), 1-5.
- 2. Nottale, L. (2011). Scale Relativity and Fractal Space-Time: A New Approach to Unifying Relativity and Quantum Mechanics. *Imperial College Press*.
- 3. Calcagni, G. (2010). Fractal universe and quantum gravity. *Physical Review Letters*, *104*(25), 251301.
- 4. El Naschie, M. S. (2004). A review of E infinity theory and the mass spectrum of high energy particle physics. *Chaos, Solitons & Fractals, 19*(1), 209-236.
- 5. Kröger, H. (2000). Fractal geometry in quantum mechanics, field theory and spin systems. *Physics Reports*, 323(2), 81-181.
- 6. Tarasov, V. E. (2011). Fractional Dynamics: Applications of Fractional Calculus to Dynamics of Particles, Fields and Media. *Springer*.
- Ambjørn, J., Jurkiewicz, J., & Loll, R. (2005). Spectral dimension of the universe. *Physical Review Letters*, 95(17), 171301.
- 8. Horava, P. (2009). Quantum gravity at a Lifshitz point. *Physical Review D*, 79(8), 084008.

- 9. Connes, A. (1994). Noncommutative Geometry. Academic Press.
- 10. Mandelbrot, B. B. (1982). The Fractal Geometry of Nature. W. H. Freeman and Company.
- 11. Wilson, K. G. (1971). Renormalization group and critical phenomena. I. Renormalization group and the Kadanoff scaling picture. *Physical Review B*, *4*(9), 3174.
- 't Hooft, G., & Veltman, M. (1972). Regularization and renormalization of gauge fields. *Nuclear Physics B*, 44(1), 189-213.
- 13. Peskin, M. E., & Schroeder, D. V. (1995). An Introduction to Quantum Field Theory. Westview Press.
- 14. Zinn-Justin, J. (2002). Quantum Field Theory and Critical Phenomena. Oxford University Press.
- 15. Weinberg, S. (1995). The Quantum Theory of Fields, Volume 1: Foundations. Cambridge University Press.
- 16. Srednicki, M. (2007). Quantum Field Theory. Cambridge University Press.
- 17. Collins, J. (1984). Renormalization: An Introduction to Renormalization, the Renormalization Group and the Operator-Product Expansion. Cambridge University Press.
- Schwartz, M. D. (2014). Quantum Field Theory and the Standard Model. Cambridge University Press.
- 19. Zee, A. (2010). Quantum Field Theory in a Nutshell. Princeton University Press.
- 20. Itzykson, C., & Zuber, J. B. (1980). Quantum Field Theory. McGraw-Hill.

**Copyright:** ©2024 Chris McGinty. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in anymedium, provided the original author and source are credited.